N. Bensalem : Sub-riemannian structure on Heisenberg group

This course is about the geometric structure of the heisenberg group. We will explain classical as well as recent results. We will develop the following aspects

Geometric properties of Heisenberg : definition of Heisenberg group, Heisenberg distribution, horizontal curves, sub-riemannian metrics, accessibility (Chow's theorem).

Geodesics of Heisenberg distribution: basic definitions and properties, Hamiltonnian approach for sub-riemannian geodesics, properties of normal geodesics, Lagrangian approach of sub-riemannian, abnormal geodesics.

Intrinsec approach connection and curvature on the Heisenberg group, properties of Carnot-Carathéodory metric, singular minimizers.